

## 12.2 Rectilinear Kinematics: Erratic Motion

From: Engineering Mechanics, Dynamics, 6th edition

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Page 17, example 12-6: A car moves along a straight line path such that its position is described by the graph shown in fig. 12-9a. Construct the v-t and a-t graphs for the time period  $0 < t < 30$ s.

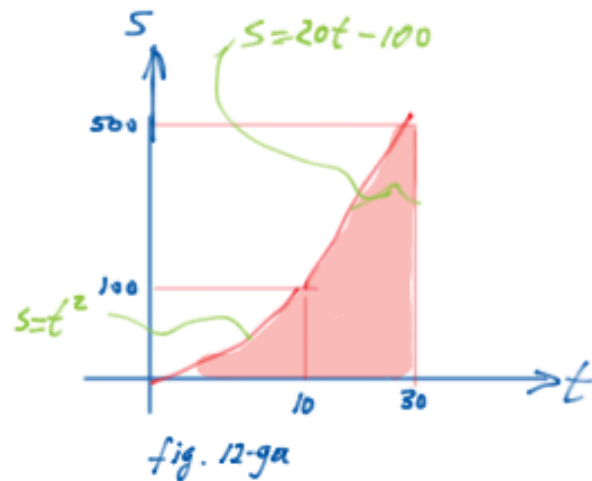
$0 \leq t \leq 10$ :

$$v = \frac{ds}{dt} \quad v = \frac{d(t^2)}{dt}$$

$$v = 2t$$

$$a = \frac{dv}{dt} \quad a = \frac{d(2t)}{dt}$$

$$a = 2$$



$10 \leq t < 30$ :

$$v = \frac{ds}{dt} \quad v = \frac{d(20t-100)}{dt}$$

$$v = 20$$

$$a = \frac{dv}{dt} \quad a = \frac{d(20)}{dt}$$

$$a = 0$$

Page 19, example 12-7: A rocket sled starts from rest and travels along a straight track such that it accelerates at a constant rate for 10s and then decelerates at a constant rate. Draw the v-t and s-t graphs and determine the time  $t'$  needed to stop the sled. How far has the sled traveled?

$0 < t < 10:$

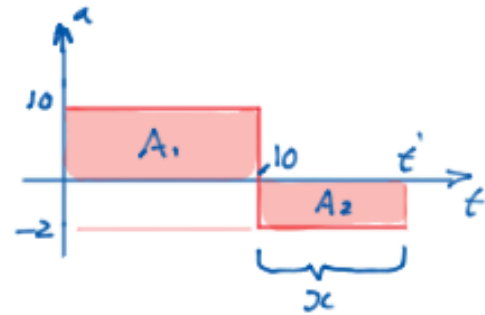
$a = \frac{dv}{dt}$

$10 = \frac{dv}{dt}$

$dv = 10 dt$

$v = 10t + C \Rightarrow @ t=0, v=0 \Rightarrow C=0$

$\rightarrow$  this equals AREA  $A_1$



$v_{(10)} = 10 \cdot 10 = 100 \text{ m/s} = A_1$   
 to stop again  $A_1 = A_2 = 100$   
 $A_2 = -2 \cdot x$   
 $100 = -2 \cdot x \Rightarrow x = 50$   
 $t' = 50 + 10 = 60 \text{ s}$

$v = \frac{ds}{dt}$

$10t = \frac{ds}{dt}$

$ds = 10 dt$

$s = 5t^2 + C \Rightarrow @ t=0, s=0 \Rightarrow C=0$

$10 < t < t':$

$a = \frac{dv}{dt}$

$-2 = \frac{dv}{dt}$

$dv = -2 dt$

$v = -2t + C \Rightarrow @ t=10, v = 10 \cdot 10 = 100 \Rightarrow 100 = -2 \cdot 10 + C$   
 $100 = -20 + C$

$C = 120$

$v = \frac{ds}{dt}$

$-2t + 120 = \frac{ds}{dt}$

$ds = (-2t + 120) dt$

$s = -t^2 + 120t + C \Rightarrow @ t=10, s = 5 \cdot 10^2 = 500 \Rightarrow 500 = -(10)^2 + 120 \cdot 10 + C$   
 $500 = -100 + 1200 + C$

$\leftarrow C = -600$

$S(60) = -(60)^2 + 120 \cdot 60 - 600$

$-3600 + 7200 - 600 = 3000 \text{ m}$

Page 21, problem 12-8: The v-s graph describing the motion of a motorcycle is shown in fig. 12-15a. Construct the a-s graph of the motion and determine the time needed for the motorcycle to reach the position  $s=400\text{ft}$ .

$0 \leq s < 200$ :

ds and dv are given  
 ds can be seen in the graph  
 the relationship between ds and dv is:  $\Rightarrow$

$$v = \frac{ds}{dt} \quad a = \frac{dv}{dt}$$

$$dt = \frac{ds}{v} \quad \& \quad dt = \frac{dv}{a}$$

$$\frac{ds}{v} = \frac{dv}{a}$$

$$a \cdot \frac{ds}{v} = dv$$

$$a \cdot ds = v \cdot dv \Rightarrow v = 0.2s + 10$$

$$a \cdot ds = (0.2s + 10) d(0.2s + 10)$$

$$a = \frac{(0.2s + 10) d(0.2s + 10)}{ds}$$

$$a = (0.2s + 10) \cdot 0.2$$

$$a = 0.04s + 2$$

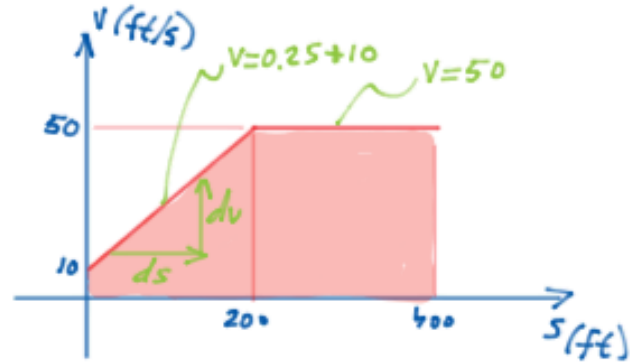


fig. 12-15a

$200 < s < 400$ :

$$v = 50$$

$$a \cdot ds = 50 \cdot d(50)$$

$$a = \frac{50 \cdot d(50)}{ds}$$

$$a = 50 \cdot 0 = 0$$

$0 \leq s < 200$ :

$$\left. \begin{array}{l} v = \frac{ds}{dt} \\ v = 0.2s + 10 \end{array} \right\} \begin{array}{l} 0.2s + 10 = \frac{ds}{dt} \\ ds = (0.2s + 10) dt \end{array}$$

$$dt = \frac{ds}{0.2s + 10}$$

@  $t=0, s=0$

$$0 = 5 \ln(10 + 0.2 \cdot 0) + C$$

$$0 = 5 \ln(10) + C$$

$$0 = 11.51 + C$$

$$C = -11.51$$

$$\leftarrow t = \frac{1}{0.2} \ln(10 + 0.2s) + C \leftarrow$$

$$\Rightarrow t_{(200)} = 5 \ln(10 + 0.2 \cdot 200) - 11.51$$

$$t_{(200)} = 5 \ln(50) - 11.51$$

$$t_{(200)} = 8.05 \text{ sec}$$

Page 556: integrals

$$\int \frac{dx}{a+bx} = \frac{1}{b} \ln(a+bx) + C$$

$$200 \leq s < 400:$$

$$v = \frac{ds}{dt}$$

$$v = 50$$

$$50 = \frac{ds}{dt}$$

$$ds = 50 dt$$

$$s = 50t + c$$

$$t = \frac{s}{50} + c \Rightarrow @ t = 8.05, s = 200$$

$$8.05 = \frac{200}{50} + c$$

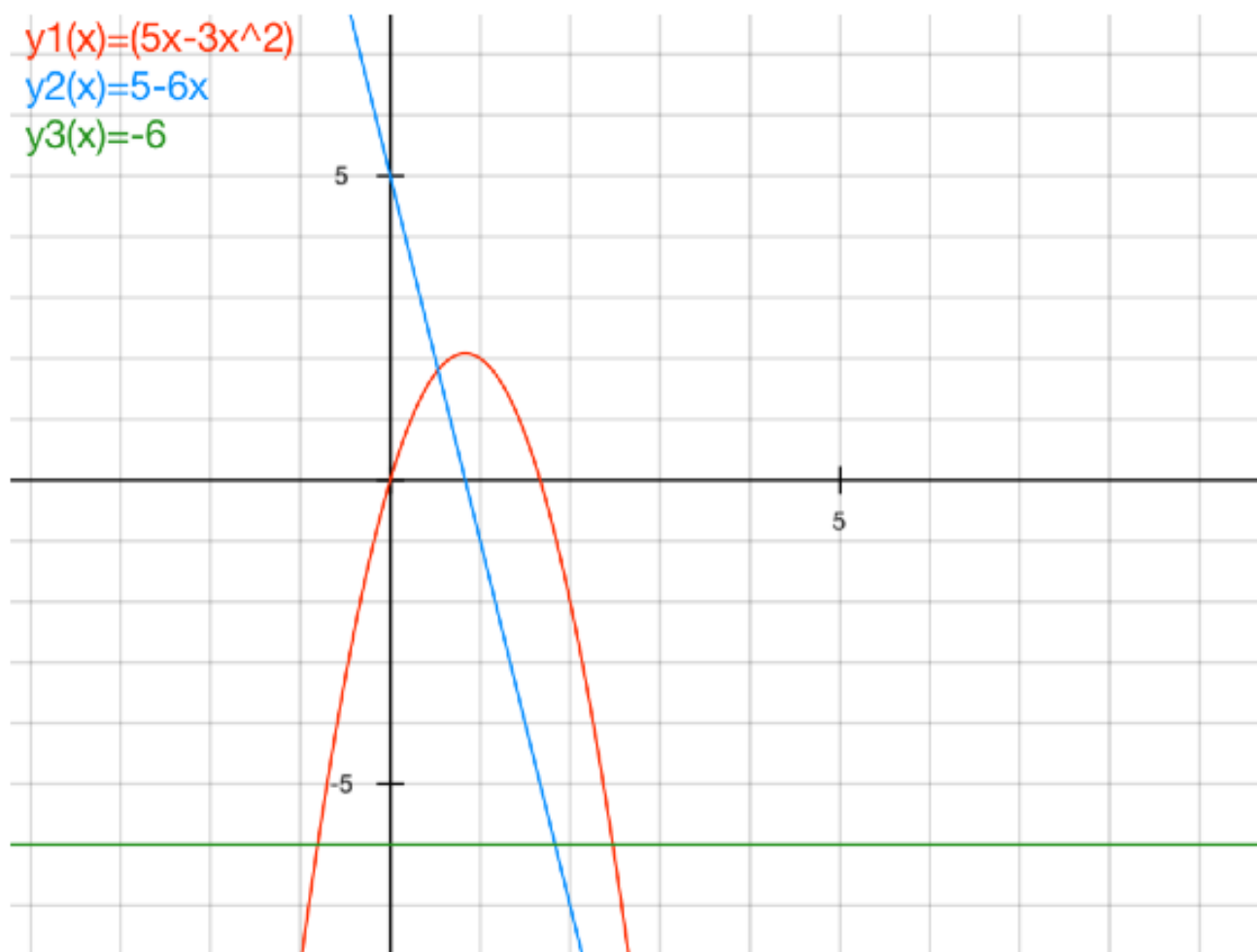
$$t(s) = \frac{s}{50} + 4.05 \quad \Leftarrow c = 4.05$$

$$t(400) = \frac{400}{50} + 4.05$$

$$= 8 + 4.05 = 12.05 \text{ sec}$$

Page 22, problem 12-31: If the position of a particle is defined as  $s=(5t-3t^2)$  ft, where  $t$  is in seconds, construct the  $s$ - $t$ ,  $v$ - $t$  and  $a$ - $t$  graph for  $0 < t < 10$  s.

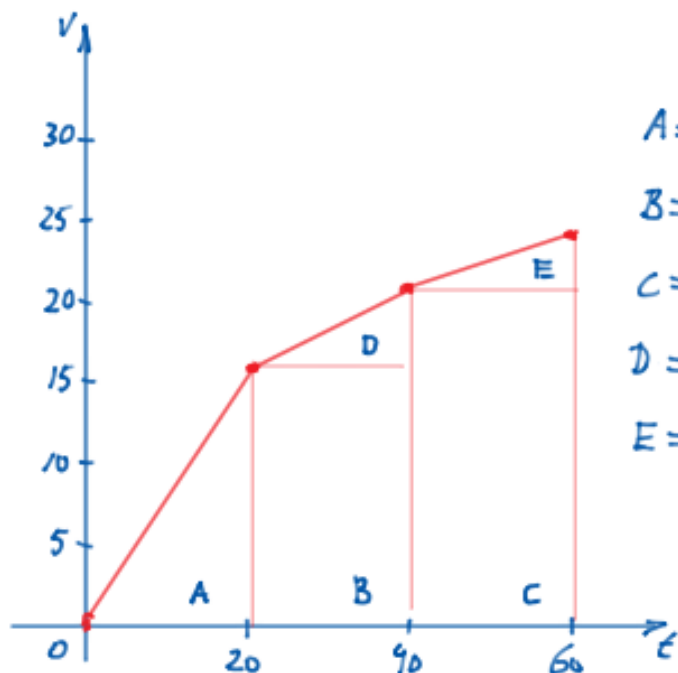
$$s = 5t - 3t^2$$
$$v = \frac{ds}{dt} = \frac{d(5t - 3t^2)}{dt} = 5 - 6t$$
$$a = \frac{dv}{dt} = \frac{d(5 - 6t)}{dt} = -6$$



Page 22, problem 12-33: The speed of a train during the first minute of its motion has been recorded as follows:

$t(s)$	0	20	40	60
$v(m/s)$	0	16	21	24

Plot the v-t graph, approximating the curve as straight line segments between the given points. Determine the total distance traveled.



$$A = \frac{20 \times 16}{2} = 160$$

$$B = 20 \times 16 = 320$$

$$C = 20 \times 21 = 420$$

$$D = \frac{20 \times 5}{2} = 50$$

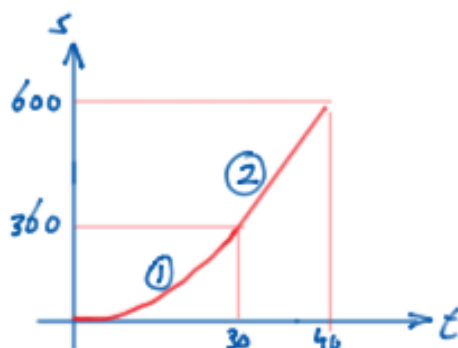
$$E = \frac{3 \times 20}{2} = 30 +$$

$$980 \text{ m} = \text{distance traveled}$$

Page 22, problem 12-34: The s-t graph for a train has been determined experimentally. From the data, construct the v-t and a-t graphs for the motion.

$$\textcircled{1} \quad s = 0.4t^2 \quad 0 \leq t < 30$$

$$\textcircled{2} \quad s = 24t - 360 \quad 30 < t < 40$$



$$v = \frac{ds}{dt} = \frac{d(0.4t^2)}{dt} = 0.8t \quad 0 \leq t < 30$$

$$v = \frac{ds}{dt} = \frac{d(24t - 360)}{dt} = 24 \quad 30 < t < 40$$

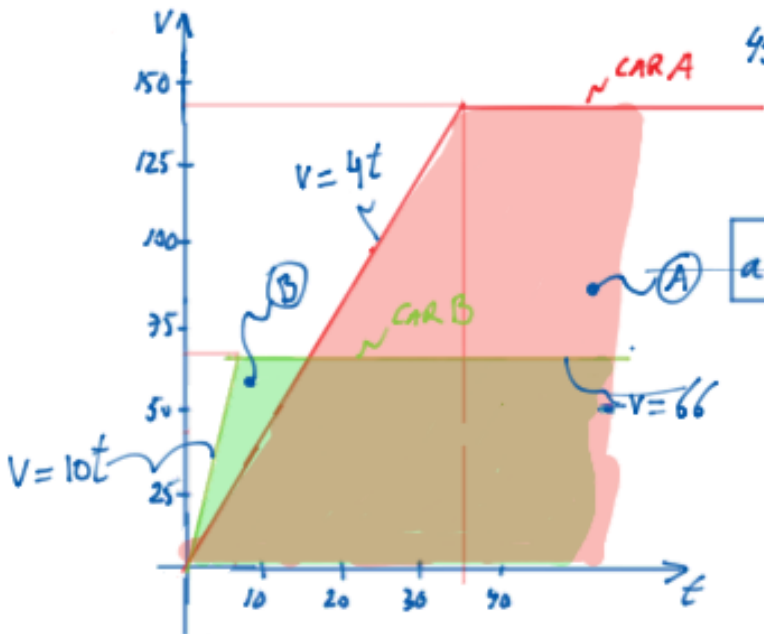
$$a = \frac{dv}{dt} = \frac{d(0.8t)}{dt} = 0.8 \quad 0 \leq t < 30$$

$$a = \frac{dv}{dt} = \frac{d(24)}{dt} = 0 \quad 30 < t < 40$$

\* ANSWER page 571,  $v = 8t$ , is wrong



Page 22, problem 12-35: Two cars start from rest side by side at the same time and position and race along a straight track. Car A accelerates at  $4 \text{ ft/s}^2$  for  $35 \text{ s}$  and then maintains a constant speed. Car B accelerates at  $10 \text{ ft/s}^2$  until reaching a speed of  $45 \text{ mi/h}$  and then maintains a constant speed. Determine the time at which the cars will again be side by side. How far has each car traveled? Construct the  $v$ - $t$  graphs for each car.



$$45 \text{ mi/h} \times 5280 = \frac{237600 \text{ ft/h}}{3600 \text{ sec}} = 66 \text{ ft/s}$$

CAR A:  $4 = \frac{dv}{dt} \Rightarrow dv = 140 \text{ ft/s}$

CAR B:  $10 = \frac{66}{dt} \Rightarrow dt = 6.6 \text{ sec}$

the cars pass each other when AREA A equals AREA B meaning both cars traveled an equal distance:

$$4t = \frac{ds}{dt}$$

$$ds = 4t \cdot dt \quad S=0 @ t=0 \Rightarrow C=0$$

$$S_A = 2t^2 + C$$

$$10t = \frac{ds}{dt}$$

$$ds = 10t \cdot dt \quad S=0 @ t=0 \Rightarrow C=0$$

$$S_B = 5t^2 + C$$

$$140 = \frac{ds}{dt}$$

$$ds = 140 dt$$

$$S_A = 140t + C$$

$$66 = \frac{ds}{dt}$$

$$ds = 66 dt$$

$$S_B = 66t + C$$

@  $t=35$ ,  $S_A = 2 \cdot 35^2 = 2450$

$$2450 = 140 \cdot 35 + C \Rightarrow C = -2450$$

$$S_A = 140t - 2450$$

@  $t=6.6$ ,  $S_B = 5 \cdot 6.6^2 = 217.8$

$$217.8 = 66 \cdot 6.6 + C \Rightarrow C = -217.8$$

$$S_B = 66t - 217.8$$

$$140t - 66t = -217.8 + 2450$$

$$74t = 2232.2 \Rightarrow t = 30.16$$

Page 22, problem 12-37: From experimental data, the motion of a jet plane while traveling along a runway is defined by the v-t graph. Construct the s-t and a-t graphs for the motion.

$0 \leq t < 5$ :  $v(t) = 4t$

$$a = \frac{dv}{dt} = \frac{d(4t)}{dt} = 4$$

$$v = \frac{ds}{dt} \Rightarrow 4t = \frac{ds}{dt}$$

$$ds = 4t \cdot dt$$

$$s = 2t^2 + C \quad [ @ t=0, s=0 \Rightarrow C=0 ]$$

$5 \leq t < 20$ :  $v(t) = 20$

$$a = 0$$

$$s = 20t + C \quad @ t=5, s = \frac{5 \times 20}{2} = 50 \Rightarrow 50 = 20 \cdot 5 + C$$

$$C = -50$$

$$s = 20t - 50$$

$20 \leq t \leq 30$ :

$$a = \frac{dv}{dt} = \frac{60-20}{30-20} = \frac{40}{10} = 4$$

$$dv = a \cdot dt = 4 \cdot dt$$

$$v = 4t + C \quad @ t=20, v=20 \Rightarrow 20 = 4 \cdot 20 + C$$

$$v = 4t - 60$$

$$C = -60$$

$$v = \frac{ds}{dt} \quad 4t - 60 = \frac{ds}{dt}$$

$$ds = (4t - 60) dt$$

$$s = 2t^2 - 60t + C$$

$$@ t=20, s = (20 \cdot 20) - 50 = 350$$

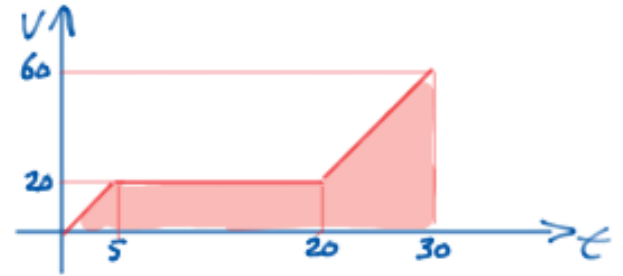
$$350 = (2 \cdot 20^2) - (60 \cdot 20) + C$$

$$350 = 800 - 1200 + C$$

$$350 = -400 + C$$

$$s = 2t^2 - 60t + 750$$

$$C = 750$$



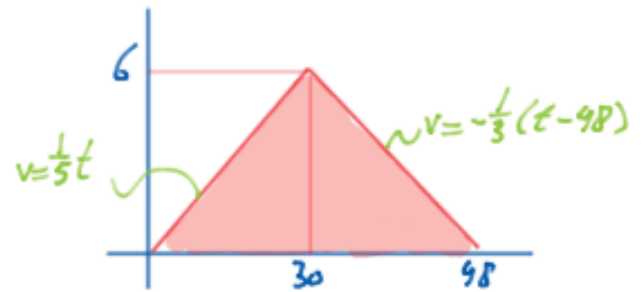
Page 23, problem 12-38: The car travels along a straight road according to the v-t graph. Determine the total distance the car travels until it stops when  $t=48\text{sec}$ . Also plot the s-t and a-t graphs.

distance traveled is area under graph:

$$s = \left(\frac{30 \cdot 6}{2}\right) + \left(\frac{(48-30) \cdot 6}{2}\right)$$

$$= 90 + 54$$

$$= 144$$



Page 23, problem 12-39: The snowmobile moves along a straight course according to the v-t graph. Construct the s-t and a-t graphs for the same 50 s time interval. When  $t=0$ ,  $s=0$ .

$$0 \leq t < 30:$$

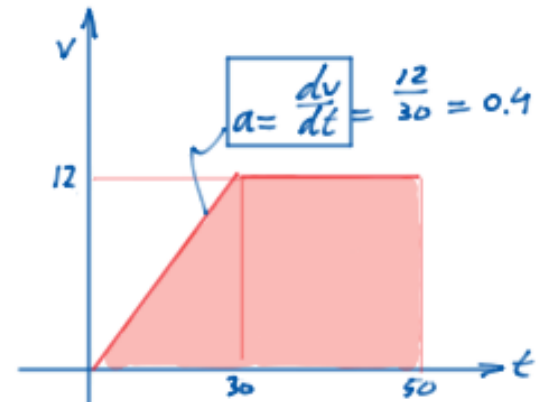
$$v(t) = 0.4t$$

$$a(t) = 0.4$$

$$v = \frac{ds}{dt} \quad 0.4t = \frac{ds}{dt}$$

$$ds = 0.4t \cdot dt$$

$$s = 0.2t^2 + C \quad [ @ t=0, s=0 \Rightarrow C=0 ]$$



$$30 \leq t < 50:$$

$$v(t) = 12$$

$$a(t) = 0$$

$$s(t) = 12t + C \quad [ @ t=30, s = 0.2 \cdot 30^2 = 180 \Rightarrow 180 = 12 \cdot 30 + C ]$$

$$180 = 360 + C$$

$$C = -180$$

$$s(t) = 12t - 180$$

Page 23, problem 12-41: The v-t graph for the motion of a car as it moves along a straight road is shown. Construct the s-t graph and determine the average speed and the distance traveled for the 30 s time interval. The car starts from rest at s=0.

$$0 \leq t < 10:$$

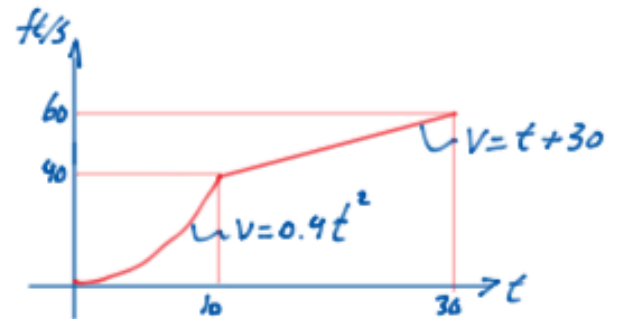
$$v(t) = 0.4t^2$$

$$v = \frac{ds}{dt} \quad 0.4t^2 = \frac{ds}{dt}$$

$$ds = 0.4t^2 \cdot dt$$

$$s = 0.13t^3 + C \Rightarrow @t=0, s=0 \Rightarrow C=0$$

$$s_{(10)} = 0.13(10^3) = 133.3 \text{ ft}$$



$$10 \leq t < 30:$$

$$v(t) = t + 30$$

$$v = \frac{ds}{dt} \quad t + 30 = \frac{ds}{dt}$$

$$ds = (t + 30) dt$$

$$ds = t \cdot dt + 30 dt$$

$$s = \frac{1}{2}t^2 + 30t + C \Rightarrow @t=10, s=133 \Rightarrow 133 = \frac{1}{2} \cdot 10^2 + 30 \cdot 10 + C$$

$$133 = 50 + 300 + C$$

$$s = \frac{1}{2}t^2 + 30t - 217$$

$\Leftrightarrow$

$$C = -217$$

$$s_{(30)} = \left(\frac{1}{2} \cdot 30^2\right) + (30 \cdot 30) - 217$$

$$= 450 + 900 - 217$$

$$= 1133 \text{ ft}$$

$$v_{\text{AVG}} = \frac{s_{\text{total}}}{t_{\text{total}}} = \frac{1133}{30} = 37.8 \text{ m/s}$$

Page 23, problem 12-42: A particle starts from rest and is subjected to the acceleration shown. Construct the v-t graph for the motion, and determine the distance traveled during the time interval  $2s < t < 6s$ .

$0 \leq t < 2$ :

$$a = 4$$

$$a = \frac{dv}{dt}$$

$$4 = \frac{dv}{dt}$$

$$dv = 4 \cdot dt$$

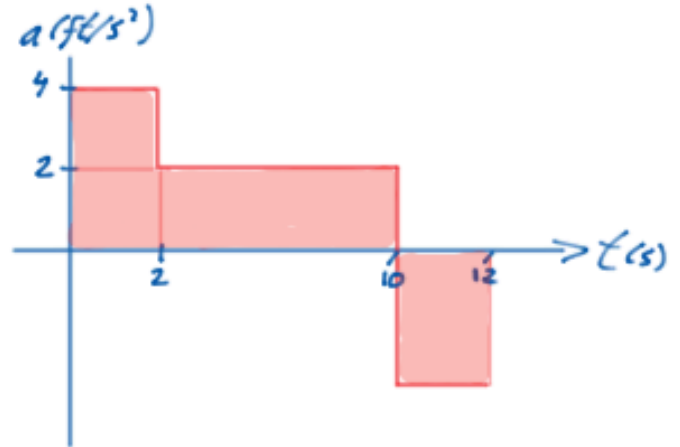
$$v = 4t + C \Rightarrow @t=0, v=0 \Rightarrow C=0$$

$$v = \frac{ds}{dt}$$

$$4t = \frac{ds}{dt}$$

$$ds = 4t \cdot dt$$

$$s = 2t^2 + C \Rightarrow @t=0, s=0 \Rightarrow C=0$$



$2 \leq t < 6$ :

$$a = 2$$

$$a = \frac{dv}{dt}$$

$$2 = \frac{dv}{dt}$$

$$dv = 2 \cdot dt$$

$$v = 2t + C \Rightarrow @t=2, v=4 \cdot 2 = 8 \Rightarrow 8 = 2 \cdot 2 + C$$

$$C = 4$$

$$v = 2t + 4$$

$$v = \frac{ds}{dt}$$

$$2t + 4 = \frac{ds}{dt}$$

$$ds = (2t + 4) dt$$

$$ds = 2t \cdot dt + 4 dt$$

$$s = t^2 + 4t + C \Rightarrow @t=2, s = 2 \cdot 2^2 = 8 \Rightarrow 8 = 2^2 + 4 \cdot 2 + C$$

$$s = t^2 + 4t - 4$$

$$C = -4 \Leftrightarrow 8 = 4 + 8 + C$$

$$\left. \begin{aligned} S(2) &= 2^2 + 4 \cdot 2 - 4 \\ &= 4 + 8 - 4 = 8 \text{ ft} \end{aligned} \right\} S(2-6) = 56 - 8 = 48 \text{ ft}$$

$$\left. \begin{aligned} S(6) &= 6^2 + 4 \cdot 6 - 4 \\ &= 36 + 24 - 4 = 56 \text{ ft} \end{aligned} \right\}$$

Page 24, problem 12-43: An airplane lands on the straight runway, originally traveling at 110ft/s when  $s=0$ . If it is subjected to the decelerations shown, determine the time  $t'$  needed to stop the plane and construct the  $s$ - $t$  graph for the motion:

$0 \leq t < 5$ : No deceleration

$$V_{(5)} = 110 \text{ ft/s}$$

$5 \leq t < 15$ : deceleration is area (A)

$$(A) = (15-5) \cdot -3 = -30$$

$$V_{(15)} = 110 - 30 = 80$$

$15 \leq t < 20$ : deceleration is area (B)

$$(B) = (20-15) \cdot -8 = -40$$

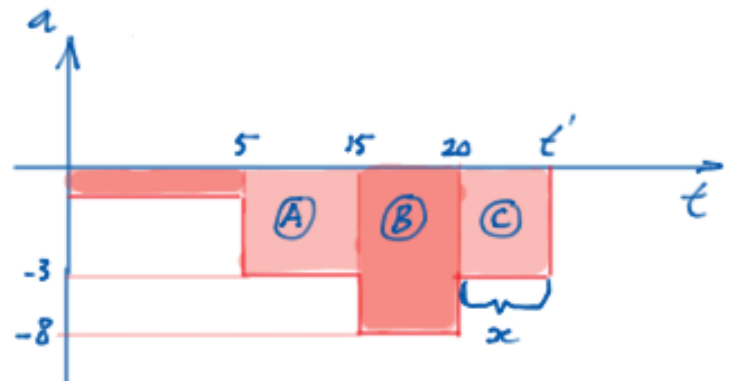
$$V_{(20)} = 80 - 40 = 40$$

$20 \leq t < t'$ : deceleration (C) = -40 (to get to 0)

$$-40 = x \cdot -3$$

$$x = 13.33$$

$$\text{total time} = 20 + 13.33 = 33.33 \text{ sec}$$



Page 24, problem 12-45: The a-t graph for a car is shown. Construct the v-t graph if the car starts from rest at t=0. At what time t' does the car stop?

$$a = \frac{dv}{dt}$$

$$\Rightarrow a = \frac{1}{2}t = \frac{dv}{dt}$$

$$dv = \frac{1}{2}t dt$$

$$v = \frac{1}{4}t^2 + C$$

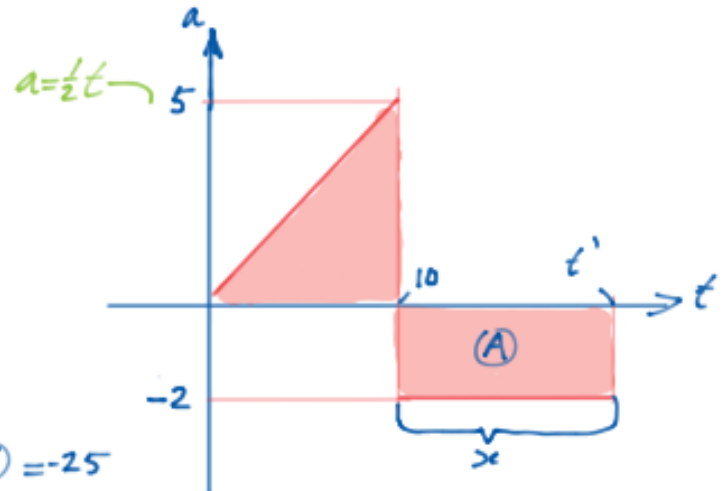
$$\text{@ } t=0, v=0 \Rightarrow C=0$$

$$\text{@ } t=10, v = \frac{1}{4}10^2 = 25$$

$$\text{deceleration to stop} = \text{AREA } \textcircled{A} = -25$$

$$x \cdot -2 = -25 \Rightarrow x = 12.5$$

$$\text{total time } t' = 12.5 + 10 = 22.5 \text{ sec}$$



Page 24, problem 12-46: A race car starting from rest travels along a straight road and for 10s has the acceleration shown. Construct the v-t graph that describes the motion and find the distance traveled in 10s.

$$0 \leq t < 6:$$

$$\frac{1}{18}t^2 = \frac{dv}{dt} \Rightarrow dv = \frac{1}{18}t^2 \cdot dt$$

$$v = \frac{1}{54}t^3 + C$$

$$\text{@ } t=0, v=0 \Rightarrow C=0$$

$$\frac{1}{18}t^3 = \frac{ds}{dt} \Rightarrow ds = \frac{1}{18}t^3 \cdot dt$$

$$s = \frac{1}{72}t^4 + C$$

$$\text{@ } t=0, s=0 \Rightarrow C=0$$

$$18 = 3 \cdot 6^2 - 24 \cdot 6 + C$$

$$18 = 108 - 144 + C$$

$$C = 54$$

$$6t - 24 = \frac{ds}{dt}$$

$$ds = (6t - 24) dt$$

$$s = 3t^2 - 24t + C$$

$$\text{@ } t=6, s = \frac{1}{72} \cdot 6^4 = 18$$

$$\begin{aligned} S_{(10)} &= 3t^2 - 24t + 54 \\ &= 3 \cdot 10^2 - 24 \cdot 10 + 54 \\ &= 300 - 240 + 54 \\ &= 114 \text{ m} \end{aligned}$$

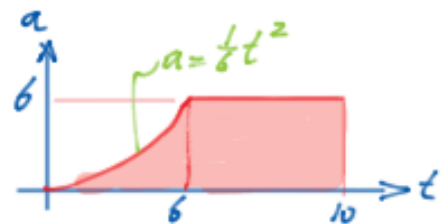
$$6 \leq t < 10:$$

$$6 = \frac{dv}{dt}$$

$$dv = 6 \cdot dt$$

$$v = 6t + C$$

$$\text{@ } t=6, v = \frac{1}{18}6^3 = 12$$



$$\Rightarrow 12 = 6t + C$$

$$12 = 6 \cdot 6 + C$$

$$12 = 36 + C$$

$$\Leftarrow C = -24$$

Page 25, problem 12-47: The boat is originally traveling at a speed of 8 m/s when it is subjected to the acceleration shown in the graph. Determine the boat's maximum speed and the time  $t$  when it stops.

$$a = \frac{dv}{dt}$$

$$-\frac{1}{4}t + 6 = \frac{dv}{dt}$$

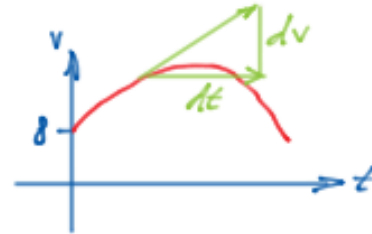
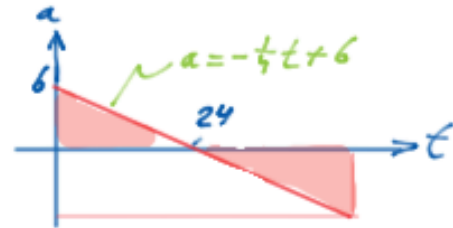
$$dv = (-\frac{1}{4}t + 6) dt$$

$$v = -\frac{1}{8}t^2 + 6t + C$$

$$\text{@ } t=0, v=8 \Rightarrow 8 = -\frac{1}{8} \cdot 0^2 + 6 \cdot 0 + C$$

$$C = 8$$

$$v = -\frac{1}{8}t^2 + 6t + 8$$



$$v_{(24)} = -\frac{1}{8} \cdot 24^2 + 6 \cdot 24 + 8$$

$$= -72 + 144 + 8$$

$$= 80 \text{ m/s}$$

$$\Leftarrow \begin{cases} v = \text{max when } \frac{dv}{dt} = 0 \\ \text{this is when } a = 0 \text{ @ } t = 24 \end{cases}$$

$$0 = -\frac{1}{8}t^2 + 6t + 8$$

$$\Leftarrow \begin{cases} \text{when the boat stops} \\ v = 0 \end{cases}$$

$$(x-8) \Rightarrow t^2 - 48t - 64 = 0$$

$$t = \frac{48 \pm \sqrt{(-48)^2 - (4 \cdot 1 \cdot -64)}}{2}$$

$$t = \frac{48 \pm \sqrt{2304 - (-256)}}{2}$$

$$t = \frac{48 \pm 50.59}{2}$$

$$t = 49.29 \text{ sec}$$

$$t = -1.29 \text{ sec}$$

$$\Leftarrow \begin{array}{|l} \text{page 555:} \\ x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \end{array}$$



Page 25, problem 12-49: The a-s graph for a race car moving along a straight track has been experimentally determined. If the car starts from rest, determine its speed when  $s=50$  ft, 150ft and 200ft, respectively.

$0 \leq s < 50$ :

$$a = \frac{dv}{dt} \quad 5 = \frac{dv}{dt}$$

$$dv = 5 \cdot dt$$

$$v = 5 \cdot t + C$$

$$\text{@ } t=0, v=0 \Rightarrow C=0$$

$$v(4.47) = 5 \cdot 4.47 = 22.36 \text{ ft/s}$$

$$v = \frac{ds}{dt} \quad 5t = \frac{ds}{dt}$$

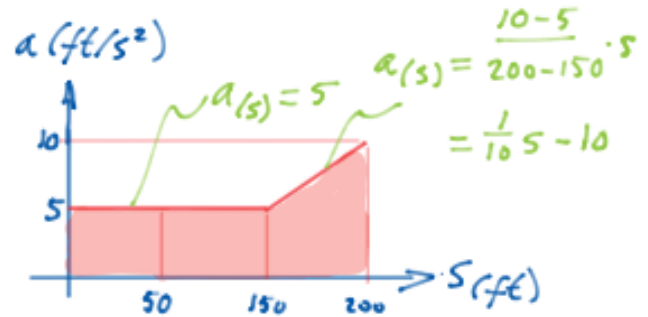
$$ds = 5t \cdot dt$$

$$s = 2.5t^2 + C$$

$$\text{@ } t=0, s=0 \Rightarrow C=0$$

$$\Downarrow$$

$$50 = 2.5t^2 \Rightarrow t = 4.47$$



$$v(7.75) = 5 \cdot 7.75 = 38.73 \text{ ft/s}$$

$$150 = 2.5t^2 \Rightarrow t = 7.75$$

$150 \leq s < 200$ :

$$a = \frac{dv}{dt} \quad \frac{1}{10}s - 10 = \frac{dv}{dt}$$

$$dt = \frac{dv}{\frac{1}{10}s - 10}$$

$$v = \frac{ds}{dt} \quad dt = \frac{ds}{v}$$

$$\frac{dv}{\frac{1}{10}s - 10} = \frac{ds}{v}$$

$$v \cdot \frac{dv}{\frac{1}{10}s - 10} = ds$$

$$v \cdot dv = \left(\frac{1}{10}s - 10\right) ds$$

$$\frac{1}{2}v^2 = \frac{1}{20}s^2 - 10s + C$$

$$\text{@ } s=150, v=38.73$$

$$\frac{1}{2} \cdot 38.73^2 = \frac{1}{20} \cdot 150^2 - 10 \cdot 150 + C$$

$$736.12 = 1125 - 1500 + C$$

$$C = 1111.12$$

$$\text{@ } s=200, v=?$$

$$\frac{1}{2}v^2 = \frac{1}{20} \cdot 200^2 - 10 \cdot 200 + 1111.12$$

$$\frac{1}{2}v^2 = 2000 - 2000 + 1111.12$$

$$v^2 = 2222.24$$

$$v = 47.14 \text{ ft/s}$$

Page 26, problem 12-53: The v-s graph for the car is given for the first 500ft of its motion. Construct the a-s graph for  $0 < s < 500$ ft. How long does it take to travel the 500ft distance? The car starts at  $s=0$  when  $t=0$ .

$$\boxed{v = \frac{ds}{dt}}$$

$$v = 0.15s + 10 \quad \left\{ \begin{array}{l} 0.15s + 10 = \frac{ds}{dt} \\ ds = (0.15s + 10) \cdot dt \\ dt = \frac{ds}{0.15s + 10} \end{array} \right.$$

$$t = \frac{1}{0.1} \ln(10 + 0.15s) + C$$

$$\text{@ } t=0, s=0$$

$$0 = 10 \ln(10) + C$$

$$0 = 23.026 + C$$

$$C = -23.026$$

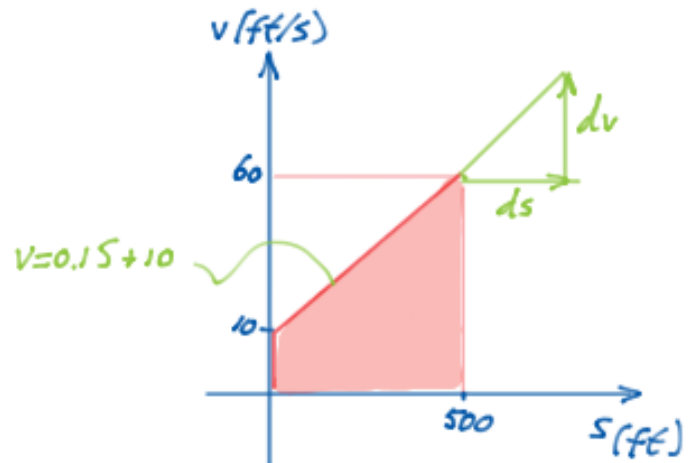
↓

$$\text{@ } s=500: t = 10 \ln(10 + 0.1 \cdot 500) - 23.026$$

$$t = 40.943 - 23.026$$

$$t = 17.92 \text{ s}$$

$$\boxed{\begin{array}{l} a=10 \\ b=0.1 \end{array}}$$



page 556, differentials:

$$\int \frac{dx}{a+bx} = \frac{1}{b} \ln(a+bx) + C$$

Page 26, problem 12-54: The  $a$ - $s$  graph for a boat moving along a straight path is given. If the boat starts at  $s=0$  when  $v=0$ , determine its speed when it is at  $s=75$ ft and 125ft respectively. Use Simpson's rule with  $n=100$  to evaluate  $v$  at  $s=125$ ft.

$0 \leq s < 100$ :

$$\left. \begin{array}{l} \boxed{a = \frac{dv}{dt}} \\ a = 5 \end{array} \right\} \begin{array}{l} s = \frac{dv}{dt} \\ dv = 5 dt \\ v = 5 \cdot t + C \end{array} \quad \left\{ \begin{array}{l} @t=0, v=0 \\ C=0 \end{array} \right.$$

$$\left. \begin{array}{l} \boxed{v = \frac{ds}{dt}} \\ v = 5t \end{array} \right\} \begin{array}{l} 5t = \frac{ds}{dt} \\ ds = 5t \cdot dt \\ s = 2.5t^2 + C \end{array} \quad \left\{ \begin{array}{l} @t=0, s=0 \\ C=0 \end{array} \right.$$

$$75(t) = 2.5t^2$$

$$t^2 =$$

$$t = 5.48 \Rightarrow v(5.48) = 5 \cdot 5.48 = 27.39$$

